

# Geometry

## Chapter 10 Review

Name Key

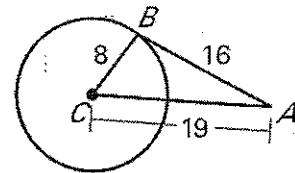
1. In the diagram,  $\overline{BC}$  is a radius of circle  $C$ . Determine whether  $\overline{AB}$  is tangent to circle  $C$ . State yes or no and show supporting work.

$$8^2 + 16^2 \stackrel{?}{=} 19^2$$

$$64 + 256 = 361$$

$$320 \neq 361$$

No,  $\overline{AB}$  is not tangent to  $\odot C$



2. In the diagram,  $\overline{AB}$  is tangent to circle  $C$  at point  $B$ . Find the radius  $r$ .

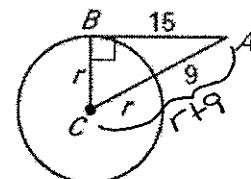
$$r^2 + 15^2 = (r+9)^2$$

$$r^2 + 225 = r^2 + 18r + 81$$

$$144 = 18r$$

$$8 = r$$

$r = 8$



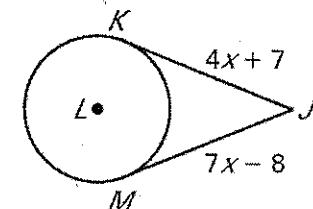
3. The points K and M are points of tangency. Find the value(s) of  $x$ .

$$4x+7 = 7x-8$$

$$15 = 3x$$

$$5 = x$$

$x = 5$



4. The points K and M are points of tangency. Find the value(s) of  $x$

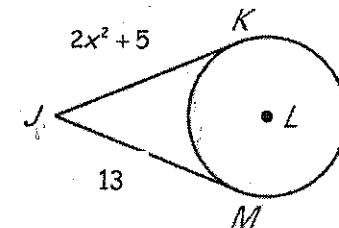
$$2x^2 + 5 = 13$$

$$2x^2 = 8$$

$$x^2 = 4$$

$$x = \pm 2$$

$x = \pm 2$



5. The points K and M are points of tangency. Find the value(s) of  $x$

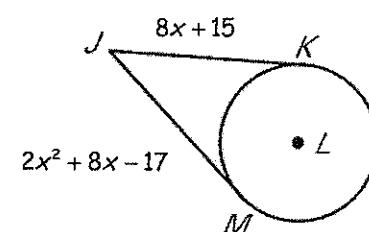
$$2x^2 + 8x - 17 = 8x + 15$$

$$2x^2 = 32$$

$$x^2 = 16$$

$$x = \pm 4$$

$x = 4$  only!



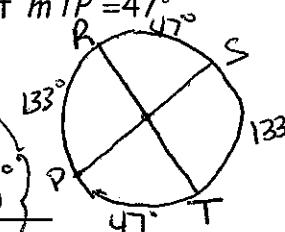
6. Two diameters of circle  $N$  are  $\overline{RT}$  and  $\overline{PS}$ . Find the given arc measure if  $m\widehat{TP} = 47^\circ$ . Draw a picture to help!

$$m\widehat{ST} = 133^\circ$$

$$m\widehat{PS} = 180^\circ$$

$$m\widehat{RTP} = 227^\circ$$

$$m\widehat{STR} = 313^\circ$$



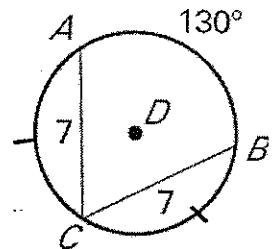
7. If there is enough information, find the measure of  $m\widehat{AC}$ .

$\cong$  chords  $\therefore \cong$  arcs

$$360 - 130 = 230$$

$$230 \div 2 = 115$$

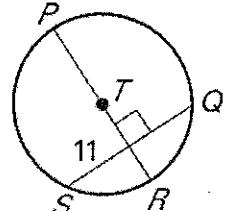
$$m\widehat{AC} = 115^\circ$$



8. If there is enough information, find the measure of chord QS.

If diameter is  $\perp$  then it bisects the chord

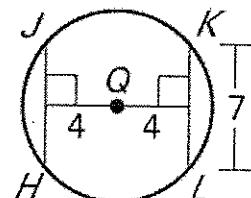
$$QS = 22$$



9. If there is enough information, find the measure of chord HJ.

If 2 chords are equidistant from center  
they are  $\cong$

$$HJ = 7$$



10. Find  $m\angle A$  and  $m\angle C$ .

$$\angle A = 45^\circ$$

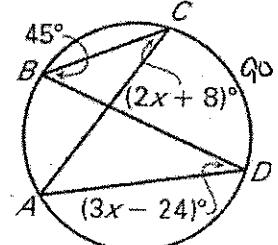
$$\angle C = 72^\circ$$

$\angle C = \angle D$  (intercept same arc)

$$2x + 8 = 3x - 24$$

$$32 = x$$

$$\angle C = 2(32) + 8 = 72^\circ$$



11. Find  $m\angle A$  and  $m\angle C$ .

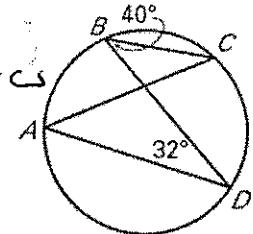
$$\angle A = 40^\circ$$

$$\angle C = 32^\circ$$

$$\angle B = \angle A$$

$$\angle C = \angle D$$

intercept same arcs



12. Find the value of the variables.

$$x = 39$$

$$y = 29$$

$$3x + 63 = 180$$

$$3x = 117$$

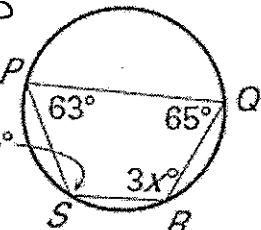
$$x = 39$$

$$4y - 1 + 65 = 180$$

$$4y = 116$$

$$y = 29$$

$$(4y - 1)^\circ$$



13. Find the value of the variables.

$$\angle F = \frac{1}{2}(96 + 45)$$

$$\angle F = 70.5^\circ$$

$$12x = \frac{1}{2}(96 + 48)$$

$$12x = 72$$

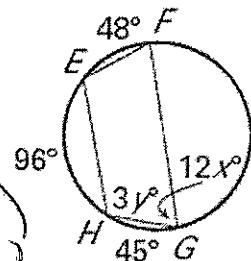
$$x = 6$$

$$3y + 70.5 = 180$$

$$3y = 109.5$$

$$y = 36.5$$

$$x = 6 \quad y = 36.5$$



Find the indicated measure in circle O, given  $m\widehat{CD} = 85^\circ$  and  $m\widehat{BE} = 97^\circ$ .

14.  $m\angle ABC = \underline{90^\circ}$

15.  $m\angle CED = \underline{42.5^\circ}$

16.  $m\angle BDE = \underline{48.5^\circ}$

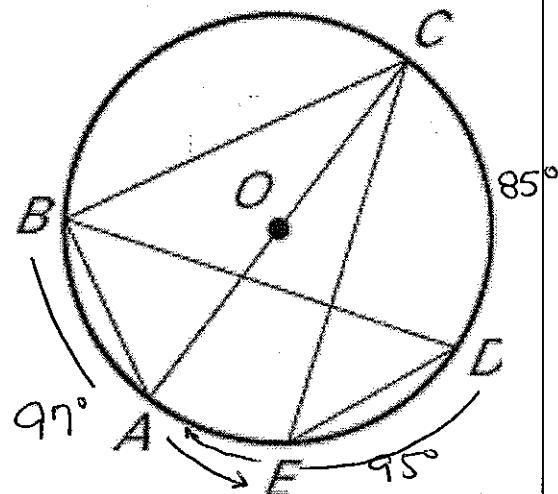
17.  $m\angle CBD = \underline{42.5^\circ}$

18.  $m\angle ABD = \underline{47.5^\circ}$

19.  $m\angle BCE = \underline{48.5^\circ}$

20.  $m\widehat{AD} = \underline{95^\circ}$

21.  $m\widehat{ABC} = \underline{180^\circ}$



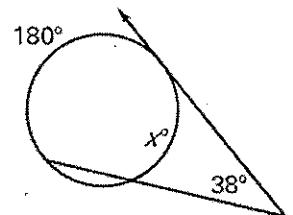
22. Find the value of x.

$$38 = \frac{1}{2}(180 - x)$$

$$76 = 180 - x$$

$$-104 = -x$$

$x = 104$



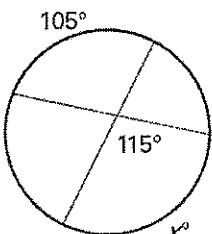
23. Find the value of x.

$$115 = \frac{1}{2}(x + 105)$$

$$230 = x + 105$$

$$125 = x$$

$x = 125$

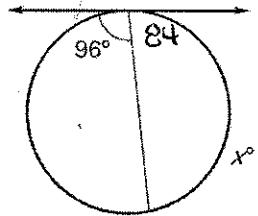


24. Find the value of x.

$$84 = \frac{1}{2}x$$

$$168 = x$$

$x = 168$



25. Find the value of x.

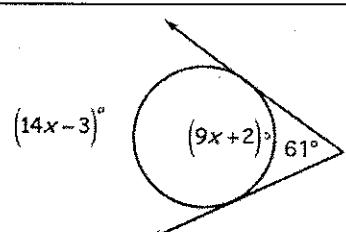
$$61 = \frac{1}{2}(14x - 3 - (9x + 2))$$

$$122 = 14x - 3 - 9x - 2$$

$$122 = 5x - 5$$

$$127 = 5x \longrightarrow x = 25.4$$

$x = 25.4$



26. The diameter of a circle is 14 feet. Exactly how far from the center of the circle is a chord that is 6 feet?

$$x^2 + 3^2 = 7^2$$

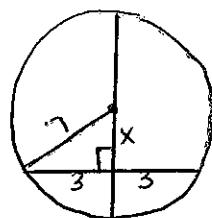
$$x^2 + 9 = 49$$

$$x^2 = 40$$

$$x = \pm \sqrt{40}$$

$$x = \pm 2\sqrt{10}$$

$x = 2\sqrt{10}$  ft



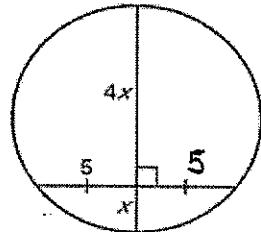
27. Find the value of  $x$ .

$$\begin{aligned}4x \cdot x &= 5 \cdot 5 \\4x^2 &= 25 \\x^2 &= \frac{25}{4}\end{aligned}$$

$$x = \pm \sqrt{\frac{25}{4}}$$

$$x = \pm 5/2$$

$$x = 5/2 \text{ or } -5/2$$

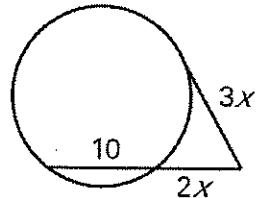


28. Find the value of  $x$ .

$$\begin{aligned}(3x)^2 &= 2x(2x+10) \\9x^2 &= 4x^2 + 20x \\5x^2 &= 20x\end{aligned}$$

$$\begin{aligned}5x^2 - 20x &= 0 \\5x(x-4) &= 0 \\5x = 0 &\quad x-4 = 0 \\x \neq 0 &\quad x = 4\end{aligned}$$

extraneous

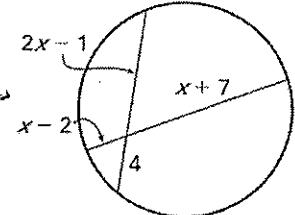


29. Find the value of  $x$ .

$$\begin{aligned}4(2x-1) &= (x-2)(x+7) \\8x-4 &= x^2 + 7x - 2x - 14 \\0 &= x^2 - 3x - 10 \\0 &= (x-5)(x+2) \\x-5 &= 0 \quad x+2 = 0\end{aligned}$$

$$x = 5 \quad x \neq -2$$

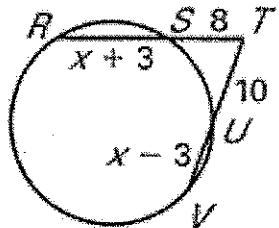
extraneous



30. Find the value of  $x$ .

$$\begin{aligned}8(x+11) &= 10(x+7) \\8x+88 &= 10x+70 \\18 &= 2x \\9 &= x\end{aligned}$$

$$x = 9$$

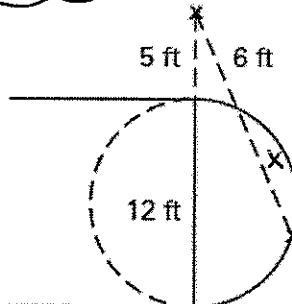


31.

**Basketball** The Xs show the positions of two basketball teammates relative to the circular "key" on a basketball court. The player outside the key passes the ball to the player on the key. To the nearest tenth of a foot, how long is the pass?

$$\begin{aligned}5(5+12) &= 6(4+x) \\5(17) &= 36 + 6x \\85 &= 36 + 6x \\49 &= 6x \\8.1666\dots &= x\end{aligned}$$

The pass is 14.2 ft



32. Given a circle:  $(x+2)^2 + (y-4)^2 = 25$

$$\begin{aligned}(-2+2)^2 + (y-4)^2 &= 25 \\0 + (y-4)^2 &= 25 \\y-4 &= \pm 5 \\y-4 &= 5 \quad y-4 = -5 \\y &= 9 \quad y = -1\end{aligned}$$

a) What is the center?  $(-2, 4)$

b) What is the length of the radius?  $5$

c) If  $(-2, y)$  is on this circle, what is/are the exact coordinate(s) of  $y$ ?  $9 \text{ or } -1$

$(-2, 9) \quad (-2, -1)$