

Absolute Value Equations

$$|x|$$

Measure Distance

$$|x-5| \neq \text{Negative #}$$

$$|2x+3| = -7$$

No Solution N/S

$$|x| = 5$$

Two answers
-5, 5

$$|x| = 0$$

one answer
Q

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$$\begin{array}{r} |x| - 3 = 10 \\ +3 +3 \end{array}$$

1st Step
Isolate $|x|$
Put BY itself

2nd Step
Remove Bars
Rewrite equation exactly
and Rewrite equation set equal
to the negative of number

$$x = 13 \quad x = -13$$

$$|2x-3| + 4 = 15$$

$$|2x-3| = 11$$

$$\begin{array}{r} 2x-3 = 11 \\ +3 +3 \end{array}$$

$$\frac{2x}{2} = \frac{14}{2}$$

$$x = 7$$

$$|2x-3| = 11$$

$$|2(-4)-3| = 11 \quad \left| \frac{2(-4)-3}{-8-3} \right| = 11$$

① Isolate

② Remove Bars
Rewrite exactly
and Rewrite set
equal to Neg. #

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$$\begin{array}{r} |5x+2|-3 = -3 \\ +3 +3 \end{array}$$

① Isolate $|x|$

$$|5x+2| = 0$$

$$\begin{array}{r} 5x+2 = 0 \\ -2 -2 \end{array}$$

$$\frac{5x}{5} = \frac{-2}{5}$$

$$x = -\frac{2}{5}$$

$$\left| 5x+2 \right| = 0$$

$$\frac{5}{1} \cdot \frac{-2}{5} = \frac{-10}{5}$$

~~$$3|2x+6| = 12$$~~

$$|2x+6| = 4$$

$$\begin{array}{r} 2x+6 = 4 \\ -6 -6 \end{array}$$

$$\frac{2x}{2} = \frac{-2}{2}$$

$$x = -1$$

$$\begin{array}{r} 2x+6 = -4 \\ -6 -6 \end{array}$$

$$\frac{2x}{2} = \frac{-10}{2}$$

$$x = -5$$

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$$\begin{aligned} \cancel{(2)} \cancel{+} |2x + 6| &= \cancel{12} \cancel{(4)} \\ |2x + 6| &= 16 \\ 2x + 6 &= 16 \quad 2x + 6 = -16 \\ \underline{-6} &\quad \underline{-6} \\ 2x &= 10 \quad 2x = -22 \\ \underline{2} &\quad \underline{2} \\ x &= 5 \quad x = -11 \end{aligned}$$

• $|5x - 1| < 9$

① Isolate $|x|$
 ② $<$ less than
 And
 ③ $>$ More OR
 ④ Remove Bars
 Rewrite exact and/or
 rewrite flip $<>$ change $\frac{1}{4}$

$$\begin{aligned} 5x - 1 &< 9 \\ 5x - 1 &\cancel{+} 1 \quad 5x - 1 &\cancel{+} 9 \\ \cancel{5x} &\cancel{+} 10 \quad \cancel{5x} &\cancel{+} 8 \\ x &\leq 2 \quad x &> -\frac{8}{5} \text{ or } -1.6 \\ \hline & -1 \frac{2}{5} < x < 2 \end{aligned}$$

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$$\begin{aligned} |x| &< 10 \quad \text{Less Than AND} \\ |x| &> 10 \quad \text{More Than OR} \end{aligned}$$

5) $|-8n| < 32$

① Isolate
 ② $<$ And
 ③ Rewrite Flip/Flip,
 $\cancel{-8n} < \cancel{32}$ AND $\cancel{-8n} > \cancel{-32}$ ↗ When
 Dividing by a Neg.
 FLIP Sign

$$\begin{aligned} n &> -4 \text{ and } n < 4 \\ \hline & -4 \quad 0 \quad 4 \end{aligned}$$

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① $\left|\frac{n}{4}\right| \leq 3$ And \rightarrow

(4) $\cancel{\frac{n}{4}} \leq 3$ AND $\cancel{\frac{n}{4}} \geq -3$

$n \leq 12$ AND $n \geq -12$

3) $\left|\frac{x}{6}\right| \geq 5$

(4) $\cancel{\frac{x}{6}} \geq 5(6)$ OR $\cancel{\frac{x}{6}} \leq -5(6)$

$x \geq 30$ OR $x \leq -30$

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Solving Equations and Inequalities
Rearranging Formulas
Independent Practice

1. Consider the following equation, $bh + hr = 25$.

Part A: Solve the equation for h .

Part B: Solve the equation for r .

2. Consider the following equation $x = \frac{r-h}{y}$.

Part A: Solve the equation for h .

Part B: Solve the equation for r .

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Equations and Inequalities
Rearranging Formulas
Mini Assessment

1. The formula for the volume of a cone is

$$V = \frac{1}{3}\pi r^2 h,$$

where r is the radius of the base and h is the height of the cone.

Part A: Solve the formula for r .

Part B: Determine the radius of the cone, if the volume of the cone is 125 cm^3 and the height of the cone is 12 cm . Round your answer to the nearest hundredth.

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